

# Wired Equivalent Privacy (WEP)

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Ma 195J.18: Principles of Cryptography

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# Introduction

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- How to send protocol data units securely from one entity to another?
- Requires both cryptography (for security) and encoding (for data integrity)

# What is WEP?

- WEP is a security protocol for wireless networks
- Based on the IEEE 802.11-1997 standard

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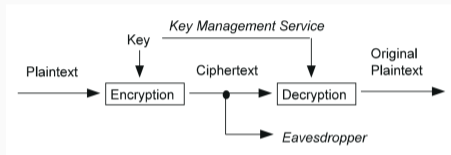
- WEP is a security protocol for wireless networks
- Based on the IEEE 802.11-1997 standard

## Goal

To provide security that equates the security mechanisms of wired local access networks (LANs)

# What is WEP?

- WEP is a symmetric-key algorithm



- Assumes that there is some Key Management Service which securely provides a copy of the same secret key to both the sender and recipient
- Details of Key Management Service not to be discussed in report, but one such way to allow secure key exchange is the Diffie-Hellman key exchange

The WEP algorithm has the following properties:

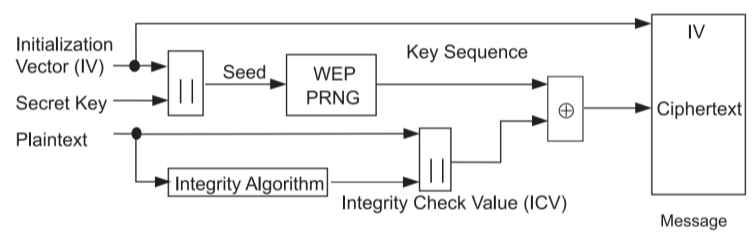
1. Reasonably strong
2. Self-synchronizing
3. Efficient
4. May be exportable
5. Optional

# Encryption and Encoding

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# Encryption process



## Encryption process

	Known by...		
	Sender	Receiver	Public
Secret Key	Yes	Yes	No
Initialization Vector	Yes	Yes	Yes (since it's useless w/o the secret key)

# Pseudorandom number generator (PRNG)

- WEP uses the **RC4** algorithm for its PRNG
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- Originally a trade secret, RC4 was leaked and then reverse-engineered in 1994

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## Thank you Bob Anderson

- To: [cynthepunks@toad.com](mailto:cynthepunks@toad.com)
- Subject: Thank you Bob Anderson
- From: [nobody@jpmix.com](mailto:nobody@jpmix.com)
- Date: Fri, 9 Sep 1994 22:11:49 -0500
- Cc: [postmaster@jpmix.com](mailto:postmaster@jpmix.com)
- Replied-By: [remailer@jpmix.com](mailto:remailer@jpmix.com)
- Sender: [cynthepunks@toad.com](mailto:cynthepunks@toad.com)

SUBJECT: RC4 Source Code

```
I've tested this. It is compatible with the RC4 object module
that comes in the various RSA toolkits.

/* rc4.h */
typedef struct rc4_key
{
    unsigned char state[256];
    unsigned char x;
    unsigned char y;
} rc4_key;
void prepare_key(unsigned char *key_data_ptr, int key_data_len,
rc4_key *key);
void rc4(unsigned char *buffer_ptr, int buffer_len, rc4_key * key);

/*rc4.c */
#include "rc4.h"
static void swap_byte(unsigned char *a, unsigned char *b);
void prepare_key(unsigned char *key_data_ptr, int key_data_len,
rc4_key *key)
{
    unsigned char swapByte;
    unsigned char index1;
```

- RC4 generates a keystream, which is a pseudorandom stream of bits
- To generate the keystream, the cipher uses an internal state which consists of two parts:
  1. A permutation of all 256 possible bytes  $S$
  2. Two 8-bit index-pointers  $i$  and  $j$

## RC4 key-scheduling algorithm

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```
1: procedure KSA( $K$ )
2:   for  $i = 0$  to 255 do
3:      $S[i] = i$ 
4:   end for
5:    $j = 0$ 
6:   for  $i = 0$  to 255 do
7:      $j = (j + S[i] + K[i \bmod K.length]) \bmod 256$ 
8:     SWAP( $S[i], S[j]$ )
9:   end for
10: end procedure
```

---

KSA is the RC4 key-scheduling algorithm, which initializes  $i$ ,  $j$ , and the permutation  $S$  based on a supplied key  $K$ .

## RC4 pseudorandom generator

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```
1:  $i = 0$ 
2:  $j = 0$ 
3: procedure PRG
4:    $i = (i + 1) \bmod 256$ 
5:    $j = (j + S[i]) \bmod 256$ 
6:   SWAP( $S[i], S[j]$ )
7:    $z = S[(S[i] + S[j]) \bmod 256]$ 
8:   return  $z$ 
9: end procedure
```

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For as many iterations as needed, the PRG updates the state and produces one byte (modulo 256) of output.

# Integrity check algorithm

- The WEP integrity check algorithm uses **CRC-32**
- CRCs are based on cyclic codes
- CRCs are popular due to ease of implementation in hardware



## Definition

Suppose that the plaintext is expressed as a polynomial  $P(x)$ . Then

$$\text{CRC}(P(x)) = x^{32}P(x) \bmod G(x)$$

where  $G(x)$  is the generator polynomial defined by

$$G(x) = x^{32} + x^{26} + x^{23} + x^{22} + x^{16} + x^{12} + x^{11} + x^{10} + x^8 + x^7 + x^5 + x^4 + x^2 + x + 1$$

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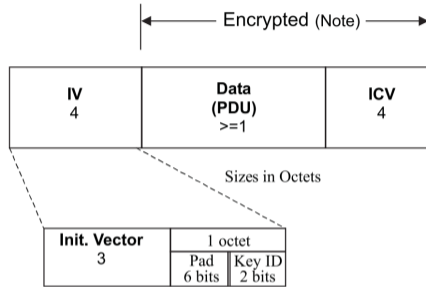
## Property

$$\text{CRC}(P(x) \oplus Q(x)) = \text{CRC}(P(x)) \oplus \text{CRC}(Q(x))$$

## **Decryption and Verification**

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# Decryption process

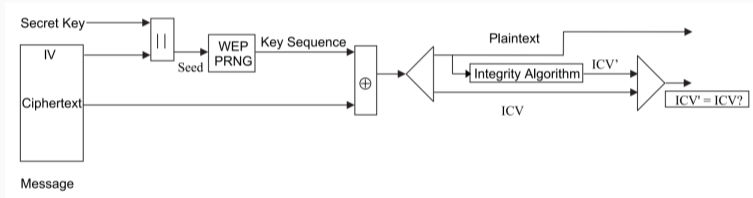


NOTE-The encipherment process has expanded the original MPDU by 8 octets, 4 for the Initialization Vector (IV) field and 4 for the Integrity Check Value (ICV). The ICV is calculated on the Data field only.

In short the receiver receives two values: (Initialization Vector, Ciphertext (contains Plaintext and CRC))

# Decryption process

Using the initialization vector, the secret key and RC4, the recipient first decrypts the ciphertext.



The recipient then verifies the recovered plaintext.

### **From §8.2.3 of the IEEE 802.11-1997 standard**

Correct decipherment shall be verified by performing the integrity check algorithm (CRC-32) on the recovered plaintext and comparing the output  $ICV'$  to the ICV transmitted with the message. If  $ICV'$  is not equal to ICV, the received MPDU is in error and an error indication is sent to MAC management.

# Vulnerabilities

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## Recap: How WEP encrypts data

- Given the plaintext (as a polynomial)  $P(x)$ , we first attach the CRC-32 checksum to it:

$$x^{32}P(x) \oplus \text{CRC}(P(x))$$

- Recall that  $\text{CRC}(P(x)) = x^{32}P(x) \bmod G(x)$
- Then the RC4 algorithm generates a key  $\text{RC4}_{\text{IV, Secret Message}}(x)$ , and we encrypt the plaintext by adding the key to it:

$$C(x) = x^{32}P(x) \oplus \text{CRC}(P(x)) \oplus \text{RC4}_{\text{IV, Secret Message}}(x)$$



- If two packets of data use the same (publicly viewable IV), then any outside party can view the message
- Recall that in WEP, the secret message is not frequently changed, only the IV is frequently changed!

- Suppose an attacker acquires the following:

$$C_1(x) = x^{32}P(x) \oplus \text{CRC}(P(x)) \oplus \text{RC4}_{\text{IV, Secret Message}}(x)$$

$$C_2(x) = x^{32}Q(x) \oplus \text{CRC}(Q(x)) \oplus \text{RC4}_{\text{IV, Secret Message}}(x)$$

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- Note that by simply adding the intercepted blocks together:

$$C_1(x) \oplus C_2(x) = x^{32}P(x) \oplus \text{CRC}(P(x)) \oplus \text{RC4}_{\text{IV, Secret Message}}(x) \\ \oplus x^{32}Q(x) \oplus \text{CRC}(Q(x)) \oplus \text{RC4}_{\text{IV, Secret Message}}(x)$$

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$$C_1(x) \oplus C_2(x) = x^{32}P(x) \oplus \text{CRC}(P(x)) \oplus x^{32}Q(x) \oplus \text{CRC}(Q(x))$$

- The packets are now vulnerable to a **known-plaintext attack**. If the attacker knows either  $P(x)$  or  $Q(x)$  then it is possible to recover the other message.

- Since the initialization vector is only 24 bits long, there are only  $2^{24} = 16777216$  choices for the IV
- Because of this, an attacker can build a decryption dictionary for all keystreams

## Unauthorized plaintext modification

- Suppose the attacker wants to modify the sent message
- Specifically: Add a polynomial  $Q(x)$  to the message
- All the attacker has to do is intercept the message and add  $x^{32}Q(x) \oplus \text{CRC}(Q(x))$  to it

# Unauthorized plaintext modification

**Proof.**

$$x^{32}P(x) \oplus \text{CRC}(P(x)) \oplus \text{RC4}_{\text{IV, Secret Message}}(x) \oplus x^{32}Q(x) \oplus \text{CRC}(Q(x))$$



# Unauthorized plaintext modification

**Proof.**

$$\begin{aligned} & x^{32}P(x) \oplus \text{CRC}(P(x)) \oplus \text{RC4}_{\text{IV, Secret Message}}(x) \oplus x^{32}Q(x) \oplus \text{CRC}(Q(x)) \\ &= (P(x) \oplus Q(x))x^{32} \oplus \text{CRC}(P(x)) \oplus \text{CRC}(Q(x)) \oplus \text{RC4}_{\text{IV, Secret Message}}(x) \end{aligned}$$





# Unauthorized plaintext modification

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## Proof.

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□

## Unauthorized plaintext modification

- The attacker has tampered with the message **and the checksum!**
- The key vulnerability is that the XOR operation used by the RC4 stream cipher is associative, and that the CRC-32 operation is linear

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### **Important!**

CRC-32 is **not a cryptographic hash function**, so it doesn't offer the security of being one-way

## Attacks on WEP

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Attacks based on statistical analysis of attempted packets have been found since 2001.




**FMS attack** (Fluhrer, Mantin, Shamir) The attack needs to intercept 4 to 6 million packets to succeed in obtaining the full secret key with a success probability of at least 50%.

**KoreK attack** The number of captured packets is reduced to about 700,000 for 50% success probability.

**PTW attack** (Pyshkin, Tews, Weinmann) The attack needs just about 35,000 to 40,000 packets for 50% success probability, which can be collected in less than 60 seconds on a fast network. Only a few seconds of CPU time is needed to execute the attack.

- The Wi-Fi Alliance announced that WEP had been superseded by Wi-Fi Protected Access (WPA) in 2003
- WEP was deprecated in 2004, with the ratification of the full 802.11i standard (a.k.a. WPA2)



-  IEEE Standard for Wireless LAN Medium Access Control (MAC) and Physical Layer (PHY) specifications.  
**IEEE Std 802.11-1997, pages 1–445, November 1997.**
-  Jiejun Kong, Mario Gerla, B.S. Prabhu, and Rajit Gadh.  
**An Overview of Network Security in WLANs.**  
*In Handbook of Wireless Local Area Networks*, pages 476–496. CRC Press, 2005.
-  Erik Tews and Martin Beck.  
**Practical attacks against WEP and WPA.**  
WiSec '09, pages 79–86, Zurich, Switzerland, 2009. ACM Press.